

# Package ‘ClassComparison’

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**Title** Classes and methods for “class comparison” problems on microarrays

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**Depends** R (>= 2.9), methods, splines, oompaBase, PreProcess, Biobase

**Description** This package defines the classes used for “class comparison” problems in the OOMPA project. Class comparison includes tests for differential expression; see Simon’s book for details on typical problem types.

**License** Artistic

**LazyLoad** yes

**URL** <http://bioinformatics.mdanderson.org/Software/OOMPA>,  
<http://bioinformatics.mdanderson.org/OOMPA>

## R topics documented:

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Bum-class

*The Bum Class***Description**

The Bum class is used to fit a beta-uniform mixture model to a set of p-values.

**Usage**

```
Bum(pvals, ...)
## S4 method for signature 'Bum':
summary(object, tau=0.01, ...)
## S4 method for signature 'Bum':
hist(x, res=100, xlab='P Values', main='', ...)
## S4 method for signature 'Bum':
image(x, ...)
## S4 method for signature 'Bum':
cutoffSignificant(object, alpha, by='FDR', ...)
## S4 method for signature 'Bum':
selectSignificant(object, alpha, by='FDR', ...)
## S4 method for signature 'Bum':
countSignificant(object, alpha, by='FDR', ...)
likelihoodBum(object)
```

**Arguments**

|        |   |
|--------|---|
| pvals  | A numeric vector containing values between 0 and 1  |
| object | A Bum object  |
| tau    | A real number between 0 and 1, representing a cutoff on the p-values.   |
| x      | A Bum object  |
| res    | A positive integer; the resolution at which to plot the fitted distribution curve.  |
| xlab   | Label for the x axis  |
| main   | Graph title   |
| alpha  | Either the false discovery rate (if by = 'FDR') or the posterior probability (if by = 'EmpiricalBayes')   |
| by     | String denoting the method to use for determining cutoffs. The choices are 'FDR', 'FalseDiscovery', or 'EmpiricalBayes'. Since the test is implemented with <a href="#">match.arg</a> , unique abbreviations also work. |
| ...    | All methods are defined to accept additional arguments in order to allow flexibility in designing derived classes. The usual graphical parameters can be supplied to <code>hist</code> and <code>image</code> .         |

## Details

The BUM method was introduced by Stan Pounds and Steve Morris, although it was simultaneously discovered by several other researchers. It is generally applicable to any analysis of microarray or proteomics data that performs a separate statistical hypothesis test for each gene or protein, where each test produces a p-value that would be valid if the analyst were only performing one statistical test. When performing thousands of statistical tests, however, those p-values no longer have the same interpretation as Type I error rates. The idea behind BUM is that, under the null hypothesis that none of the genes or proteins is interesting, the expected distribution of the set of p-values is uniform. By contrast, if some of the genes are interesting, then we should see an overabundance of small p-values (or a spike in the histogram near zero). We can model the alternative hypothesis with a beta distribution, and view the set of all p-values as a mixture distribution.

Fitting the BUM model is straightforward, using a nonlinear optimizer to compute the maximum likelihood parameters. After the model has been fit, one can easily determine cutoffs on the p-values that correspond to desired false discovery rates. Alternatively, the original Pounds and Morris paper shows that their results can be reinterpreted to recover the empirical Bayes method introduced by Efron and Tibshirani. Thus, one can also determine cutoffs by specifying a desired posterior probability of significance.

## Value

Graphical functions (`hist` and `image`) invisibly return the object on which they were invoked.

The `cutoffSignificant` method returns a real number between zero and one. P-values below this cutoff are considered statistically significant at either the specified false discovery rate or at the specified posterior probability.

The `selectSignificant` method returns a vector of logical values whose length is equal to the length of the vector of p-values that was used to construct the `Bum` object. True values in the return vector mark the statistically significant p-values.

The `countSignificant` method returns an integer, the number of statistically significant p-values.

The `summary` method returns an object of class `BumSummary`.

## Creating Objects

Although objects can be created directly using `new`, the most common usage will be to pass a vector of p-values to the `Bum` function.

## Slots

**pvals:** The vector of p-values used to construct the object.

**ahat:** Model parameter

**lhat:** Model parameter

**pihat:** Model parameter

## Methods

**summary(object, tau=0.01, ...)** For each value of the p-value cutoff `tau`, computes estimates of the fraction of true positives (TP), false negatives (FN), false positives (FP), and true negatives (TN).

**hist(x, res=100, xlab='P Values', main='', ...)** Plots a histogram of the object, and overlays (1) a straight line to indicate the contribution of the uniform component and (2) the fitted beta-uniform distribution from the observed values. Colors in the plot are controlled by `COLOR.EXPECTED` and `COLOR.OBSERVED`.

**image(x, ...)** Produces four plots in a 2x2 layout: (1) the histogram produced by `hist`; (2) a plot of cutoffs against the desired false discovery rate; (3) a plot of cutoffs against the posterior probability of coming from the beta component; and (4) an ROC curve.

**cutoffSignificant(object, alpha, by='FDR', ...)** Computes the cutoff needed for significance, which in this case means arising from the beta component rather than the uniform component of the mixture. Significance is specified either by the false discovery rate (when `by = 'FDR'` or `by = 'FalseDiscovery'`) or by the posterior probability (when `by = 'EmpiricalBayes'`)

**selectSignificant(object, alpha, by='FDR', ...)** Uses `cutoffSignificant` to determine a logical vector that indicates which of the p-values are significant.

**countSignificant(object, alpha, by='FDR', ...)** Uses `selectSignificant` to count the number of significant p-values.

### Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

### References

Pounds S, Morris SW. Estimating the occurrence of false positives and false negatives in microarray studies by approximating and partitioning the empirical distribution of p-values. *Bioinformatics*. 2003 Jul 1;19(10):1236-42.

Benjamini Y, Hochberg Y. Controlling the false discovery rate: a practical and powerful approach to multiple testing. *J Roy Statist Soc B*, 1995; 57: 289-300.

Efron B, Tibshirani R: Empirical bayes methods and false discovery rates for microarrays. *Genet Epidemiol* 2002, 23: 70-86.

### See Also

Two classes that produce lists of p-values that can (and often should) be analyzed using BUM are [MultiTtest](#) and [MultiLinearModel](#). Also see [BumSummary](#).

### Examples

```
fake.data <- c(runif(700), rbeta(300, 0.3, 1))
a <- Bum(fake.data)
hist(a, res=200)

alpha <- (1:25)/100
plot(alpha, cutoffSignificant(a, alpha, by='FDR'),
      xlab='Desired False Discovery Rate', type='l',
      main='FDR Control', ylab='Significant P Value')

GAMMA <- 5*(10:19)/100
plot(GAMMA, cutoffSignificant(a, GAMMA, by='EmpiricalBayes'),
      ylab='Significant P Value', type='l',
      main='Empirical Bayes', xlab='Posterior Probability')

b <- summary(a, (0:100)/100)
be <- b@estimates
```

```
sens <- be$TP/(be$TP+be$FN)
spec <- be$TN/(be$TN+be$FP)
plot(1-spec, sens, type='l', xlim=c(0,1), ylim=c(0,1), main='ROC Curve')
points(1-spec, sens)
abline(0,1)

image(a)

countSignificant(a, 0.05, by='FDR')
countSignificant(a, 0.99, by='Emp')

#cleanup
rm(a, b, be, alpha, GAMMA, sens, spec, fake.data)
```

---

BumSummary-class     *The BumSummary class*

---

## Description

An implementation class. Users are not expected to create these objects directly; they are produced as return objects from the summary method for Bum.

## Slots

**bum:** Object of class Bum  
**estimates:** Object of class data.frame  
**Fhat:** Object of class numeric

## Methods

**show** signature(object = "BumSummary"): Print the object, which contains a summary of the underlying Bum object. The summary contains a data frame with estimates of the fraction of true positives (TP), false positives (FP), true negatives (TN) and false negatives (FN) at the set of p-value cutoffs specified in the call to the summary method.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## See Also

[Bum](#)

## Examples

```
# See the examples for the Bum class.
```

Dudoit-class

*The Dudoit Class***Description**

An implementation of the method of Dudoit and colleagues to apply the Westfall-Young adjustment to p-values to control the family-wise error rate when analyzing microarray data.

**Usage**

```
Dudoit(data, classes, nPerm = 1000, verbose = TRUE)
## S4 method for signature 'Dudoit, missing':
plot(x, ylab='T statistics', ...)
## S4 method for signature 'Dudoit':
cutoffSignificant(object, alpha, ...)
## S4 method for signature 'Dudoit':
selectSignificant(object, alpha, ...)
## S4 method for signature 'Dudoit':
countSignificant(object, alpha, ...)
```

**Arguments**

|         |   |
|---------|---|
| data    | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| nPerm   | An integer; the number of permutations to perform   |
| verbose | A logical flag  |
| object  | A Dudoit object   |
| alpha   | A real number; the target family-wise error rate  |
| x       | A Dudoit object   |
| ylab    | Label for the y axis  |
| ...     | The usual extra arguments for generic or plotting routines.   |

**Details**

In 2002, Dudoit and colleagues introduced a method to adjust the p-values when performing gene-by-gene tests for differential expression. The adjustment was based on the method of Westfall and Young, with the goal of controlling the family-wise error rate.

**Value**

The standard method for `plot` returns what you would expect.

The `cutoffSignificant` method returns a real number (its input value `alpha`). The `selectSignificant` method returns a vector of logical values identifying the significant test results, and `countSignificant` returns an integer counting the number of significant test results.

## Objects from the Class

As usual, objects can be created by `new`, but better methods are available in the form of the `Dudoit` function. The basic inputs to this function are the same as those used for row-by-row statistical tests throughout the `ClassComparison` package; a detailed description can be found in the `MultiTtest` class.

The additional input determines the number, `nPerm`, of permutations to perform. The accuracy of the p-value adjustment depends on this value. Since the implementation is in R (and does not call out to something compiled like C or FORTRAN), however, the computations are slow. The default value of 1000 can take a long time with modern microarrays that contain 40,000 spots.

## Slots

**adjusted.p:** The numeric vector of adjusted p-values.

**t.statistics:** Object of class `numeric` containing the computed t-statistics.

**p.values:** Object of class `numeric` containing the computed p-values.

**groups:** Object of class `character` containing the names of the classes being compared.

**call:** Object of class `call` containing the function call that created the object.

## Extends

Class `MultiTtest`, directly. In particular, objects of this class inherit methods for `summary`, `hist`, and `plot` from the base class.

## Methods

**cutoffSignificant(object, alpha, ...)** Determine cutoffs on the adjusted p-values at the desired significance level. In other words, this function simply returns `alpha`.

**selectSignificant(object, alpha, ...)** Compute a logical vector for selecting significant test results.

**countSignificant(object, alpha, ...)** Count the number of significant test results.

**plot** `signature(x = Dudoit, y = missing):...`

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Dudoit, S., Y.H. Yang, M.J. Callow, and T.P. Speed. 2002. Statistical Methods for Identifying Differentially Expressed Genes in Replicated cDNA Microarray Experiments, *Statistica Sinica*, 12(1): 111-139.

Westfall, P.H., Young, S.S. Resampling-based multiple testing: examples and methods for p-value adjustment. Wiley series in probability and mathematics statistics. John Wiley and Sons, 1993.

## See Also

[MultiTtest](#), [Bum](#), [SmoothTtest](#)

**Examples**

```

ng <- 10000
ns <- 15
nd <- 200
fake.class <- factor(rep(c('A', 'B'), each=ns))
fake.data <- matrix(rnorm(ng*ns*2), nrow=ng, ncol=2*ns)
fake.data[1:nd, 1:ns] <- fake.data[1:nd, 1:ns] + 2
fake.data[(nd+1):(2*nd), 1:ns] <- fake.data[(nd+1):(2*nd), 1:ns] - 2

# the permutation test is slow. it really needs more than
# 100 permutations, but this is just an example...
dud <- Dudoit(fake.data, fake.class, nPerm=100)
summary(dud)
plot(dud)
countSignificant(dud, 0.05)

rm(ng, ns, nd, fake.class, fake.data, dud)

```

---

dwil

*Wilcoxon Density Function*


---

**Description**

Computes the density function for the Wilcoxon rank-sum distribution without centering.

**Usage**

```
dwil(q, m, n)
```

**Arguments**

|   |   |
|---|---|
| q | vector of quantiles                         |
| m | number of observations in the first sample  |
| n | number of observations in the second sample |

**Details**

Computes the density function for the Wilcoxon rank-sum distribution, using exact values when both groups have fewer than 50 items and switching to a normal approximation otherwise. It was originally written for S-Plus, which still perversely insists that *m* and *n* must be less than 50. The function was retained when the OOMPA library was ported to R, since S-Plus keeps the actual rank-sum but R centers the distribution at zero. This function encapsulated the difference, allowing everything else to continue to work as it had worked previously.

**Value**

A vector of the same length as *q* containing (approximate or exact) values of the density function.

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**See Also**

[MultiWilcoxonTest](#)

**Examples**

```
dwil(51:60, 9, 3)
dwil(51:60, 9, 51)
```

---

matrixT

*Multiple T Tests by Matrix Multiplication*

---

**Description**

Utility functions for computing vectors of row-by-row means, variances, and t-statistics.

**Usage**

```
matrixMean(x, na.rm=FALSE)
matrixUnequalT(m, v)
matrixPairedT(m, v, pf)
matrixVar(x, xmean, na.rm=FALSE)
matrixT(m, v, na.rm=FALSE)
```

**Arguments**

|                    |  |
|--------------------|--|
| <code>x</code>     | a matrix   |
| <code>xmean</code> | a numeric vector or single-column matrix   |
| <code>m</code>     | a matrix   |
| <code>na.rm</code> | a logical value indicating whether means, variances, and t-statistics should be computed after omitting NA values from individual rows of the data matrix. |
| <code>v</code>     | a logical vector of length equal to the number of columns of <code>m</code>  |
| <code>pf</code>    | a numerical vector of length equal to the number of columns of <code>m</code> , indicating which samples should be paired                                  |

**Value**

`matrixMean` returns a single-column matrix containing the row-by-row means of `x`.

`matrixVar` returns a single-column matrix containing the row-by-row means of `x`, assuming that `xmean` contains the corresponding mean values.

`matrixT` returns a single-column matrix of t-statistics from a two-sample t-test comparing the columns for which `v` is true to those for which `v` is false.

`matrixPairedT` returns a single-column matrix of t-statistics from a paired t-test.

`matrixUnequalT` returns a list with two components: `tt` is a single-column matrix of t-statistics from a two-sample unequal variance t-test comparing the columns for which `v` is true to those for which `v` is false, and `df` is a single-column matrix of the degrees of freedom associated with each row..

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**See Also**

[MultiTtest](#)

**Examples**

```
ng <- 1000
ns <- 50
dat <- matrix(rnorm(ng*ns), ncol=ns)
clas <- factor(rep(c('Good', 'Bad'), each=25))
myMean <- matrixMean(dat)
myVar <- matrixVar(dat, myMean)
plot(myMean, myVar)

myT <- matrixT(dat, clas)
hist(myT)

rm(ng, ns, dat, myMean, myVar, myT)
```

---

MultiLinearModel-class

*The MultiLinearModel Class*

---

**Description**

Class to fit multiple (row-by-row) linear (fixed-effects) models on microarray or proteomics data.

**Usage**

```
MultiLinearModel(form, clindata, arraydata)
## S4 method for signature 'MultiLinearModel':
summary(object, ...)
## S4 method for signature 'MultiLinearModel':
hist(x, xlab='F Statistics', main=NULL, ...)
## S4 method for signature 'MultiLinearModel, missing':
plot(x, ylab='F Statistics', ...)
## S4 method for signature 'MultiLinearModel, ANY':
plot(x, y, xlab='F Statistics',
     ylab=deparse(substitute(y)), ...)
## S4 method for signature 'MultiLinearModel':
anova(object, ob2, ...)
multiTukey(object, alpha)
```

**Arguments**

|          |   |
|----------|---|
| form     | A formula object specifying the linear model  |
| clindata | Either a data frame of "clinical" or other covariates or an <a href="#">ExpressionSet</a> . |

|                        |   |
|------------------------|---|
| <code>arraydata</code> | A matrix or data frame of values to be explained by the model. If <code>clindata</code> is an <code>ExpressionSet</code> , then <code>arraydata</code> can be omitted, since it is assumed to be part of the <code>ExpressionSet</code> . |
| <code>object</code>    | A <code>MultiLinearModel</code> object  |
| <code>ob2</code>       | Another <code>MultiLinearModel</code> object  |
| <code>x</code>         | A <code>MultiLinearModel</code> object  |
| <code>y</code>         | A numeric vector  |
| <code>xlab</code>      | Label for the x-axis  |
| <code>ylab</code>      | Label for the y-axis  |
| <code>main</code>      | Graph title   |
| <code>...</code>       | Optional graphical or other parameters to generic functions   |
| <code>alpha</code>     | A real number between 0 and 1; the significance level for the Tukey test.   |

### Value

The `anova` method returns a data frame. The rows in the data frame corresponds to the rows in the `arraydata` object that was used to construct the `MultiLinearModel` objects. The first column contains the F-statistics and the second column contains the p-values.

The `multiTukey` function returns a vector whose length equals the number of rows in the `arraydata` object used to construct the `MultiLinearModel`. Assuming that the overall F-test was significant, differences in group means (in each data row) larger than this value are significant by Tukey's test for honestly significant difference. (Of course, that statement is incorrect, since we haven't fully corrected for multiple testing. Our standard practice is to take the p-values from the row-by-row F-tests and evaluate them using the beta-uniform mixture model (see [Bum](#)). For the rows that correspond to models whose p-values are smaller than the `Bum` cutoff, we simply use the Tukey HSD values without further modification.)

### Creating Objects

Objects should be created by calling the `MultiLinearModel` function. The first argument is a [formula](#) specifying the linear model, in the same manner that it would be passed to `lm`. We will fit the linear model separately for each row in the `arraydata` matrix. Rows of `arraydata` are attached to the `clindata` data frame and are always referred to as "Y" in the formulas. In particular, this implies that `clindata` can not include a column already called "Y". Further, the implementation only works if "Y" is the response variable in the model.

### Multiple linear models with "ExpressionSet" objects

The BioConductor packages uses an `ExpressionSet` to combine microarray data and clinical covariates (known in their context as `phenoData` objects) into a single structure. You can call `MultiLinearModel` using an `ExpressionSet` object for the `clindata` argument. In this case, the function extracts the `phenoData` slot of the `ExpressionSet` to use for the clinical covariates, and extracts the `exprs` slot of the `ExpressionSet` object to use for the array data.

### Slots

**call:** A `call` object describing how the object was constructed.

**model:** The `formula` object specifying the linear model.

**F.statistics:** A numeric vector of F-statistics comparing the linear model to the null model.

**p.values:** A numeric vector containing the p-values associated to the F-statistics.

**coefficients:** A `matrix` of the coefficients in the linear models.

**predictions:** A `matrix` of the (Y-hat) values predicted by the models.

**sse:** A numeric vector of the sum of squared error terms from fitting the models.

**ssr:** A numeric vector of the sum of squared regression terms from the model.

**df:** A numeric vector (of length two) containing the degrees of freedom for the F-tests.

## Methods

**summary(object, ...)** Write out a summary of the object.

**hist(x, xlab='F Statistics', main=NULL, ...)** Create a histogram of the F-statistics.

**plot(x, ylab='F Statistics', ...)** Plot the F-statistics as a function of the row index.

**plot(x, y, xlab='F Statistics', ylab=deparse(substitute(y)), ...)** Plot the F-statistics against the numeric vector `y`.

**anova(object, ob2, ...)** Perform row-by-row F-tests comparing two different linear models.

## Details

The `MultiLinearModel` constructor computes row-by-row F-tests comparing each linear model to the null model  $Y \sim 1$ . In many instances, one wishes to use an F-test to compare two different linear models. For instance, many standard applications of analysis of variance (ANOVA) can be described using such a comparison between two different linear models. The `anova` method for the `MultiLinearModel` class performs row-by-row F-tests comparing two competing linear models.

The implementation of `MultiLinearModel` does not take the naive approach of using either `apply` or a `for`-loop to attach rows one at a time and fit separate linear models. All the models are actually fit simultaneously by a series of matrix operations, which greatly reduces the amount of time needed to compute the models. The constraint on the column names in `clindata` still holds, since one row is attached to allow `model.matrix` to determine the contrasts matrix.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## See Also

[MultiTtest](#), [MultiWilcoxonTest](#), [Bum](#), [lm](#), [anova](#).

## Examples

```
ng <- 10000
ns <- 50
dat <- matrix(rnorm(ng*ns), ncol=ns)
cla <- factor(rep(c('A', 'B'), 25))
cla2 <- factor(rep(c('X', 'Y', 'Z'), times=c(15, 20, 15)))
covars <- data.frame(Grade=cla, Stage=cla2)
res <- MultiLinearModel(Y ~ Grade + Stage, covars, dat)
summary(res)
hist(res, breaks=101)
plot(res)
plot(res, res@p.values)
```

```

graded <- MultiLinearModel(Y ~ Grade, covars, dat)
summary(graded)

hist(graded@p.values, breaks=101)
hist(res@p.values, breaks=101)

oop <- anova(res, graded)
hist(oop$p.values, breaks=101)

# cleanup
rm(ng, ns, dat, cla, cla2, covars, res, graded, oop)

```

---

MultiTtest-class      *The MultiTtest Class*

---

## Description

Class to perform row-by-row t-tests on microarray or proteomics data.

## Usage

```

MultiTtest(data, classes, na.rm=TRUE)
## S4 method for signature 'MultiTtest':
summary(object, ...)
## S4 method for signature 'MultiTtest':
as.data.frame(x, row.names = NULL, optional = FALSE, ...)
## S4 method for signature 'MultiTtest':
hist(x, xlab='T Statistics', main=NULL, ...)
## S4 method for signature 'MultiTtest, missing':
plot(x, ylab='T statistics', ...)
## S4 method for signature 'MultiTtest, ANY':
plot(x, y, xlab='T Statistics', ylab=deparse(substitute(y)), ...)

```

## Arguments

|         |   |
|---------|---|
| data    | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| na.rm   | a logical value indicating whether t-statistics should be computed after omitting NA values from individual rows of the data matrix.  |
| object  | A <a href="#">MultiTtest</a> object   |
| x       | A <a href="#">MultiTtest</a> object   |
| y       | A numeric vector  |
| xlab    | Label for the x axis  |
| ylab    | Label for the y axis  |
| main    | Plot title  |

`row.names` see the base version  
`optional` see the base version  
`...` The usual graphical parameters can be supplied to `hist` and `plot` methods.

### Value

The graphical routines invisibly return the object against which they were invoked.

### Creating objects

Although objects can be created using `new`, the better method is to use the `MultiTtest` function. In the simplest case, you simply pass in a data matrix and a logical vector assigning classes to the columns, and the constructor performs row-by-row two-sample t-tests and computes the associated (single test) p-values. To adjust for multiple testing, you can pass the p-values on to the `Bum` class.

If you use a factor instead of a logical vector, then the t-test compares the first level of the factor to everything else. To handle the case of multiple classes, see the `MultiLinearModel` class.

As with other class comparison functions that are part of the OOMPA, we can also perform statistical tests on `ExpressionSet` objects from the BioConductor libraries. In this case, we pass in an `ExpressionSet` object along with the name of a factor to use for splitting the data.

### Slots

**t.statistics:** Object of class `numeric` containing the computed t-statistics.

**p.values:** Object of class `numeric` containing the computed p-values.

**groups:** Object of class `character` containing the names of the classes being compared.

**call:** Object of class `call` containing the function call that created the object.

### Methods

**summary(object, ...)** Write out a summary of the object.

**hist(x, xlab='T Statistics', main=NULL, ...)** Produce a histogram of the t-statistics.

**plot(x)** Produces a scatter plot of the t-statistics against their index.

**plot(x,y)** Produces a scatter plot of the t-statistics in the object `x` against the numeric vector `y`.

### Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

### See Also

[matrixT](#), [Bum](#), [MultiLinearModel](#), [Dudoit](#)

### Examples

```
ng <- 10000
ns <- 50
dat <- matrix(rnorm(ng*ns), ncol=ns)
cla <- factor(rep(c('A', 'B'), each=25))
res <- MultiTtest(dat, cla)
summary(res)
hist(res, breaks=101)
plot(res)
```

```

plot(res, res@p.values)
hist(res@p.values, breaks=101)

dat[1,1] <- NA
mm <- matrixMean(dat, na.rm=TRUE)
vv <- matrixVar(dat, mm, na.rm=TRUE)
tt <- matrixT(dat, cla, na.rm=TRUE)
mtt <- MultiTtest(dat, cla)

rm(ng, ns, dat, cla, res)

```

---

MultiWilcoxonTest-class

*The MultiWilcoxonTest Class*


---

## Description

The MultiWilcoxonTest class is used to perform row-by-row Wilcoxon rank-sum tests on a data matrix. Significance cutoffs are determined by the empirical Bayes method of Efron and Tibshirani

## Usage

```

MultiWilcoxonTest(data, classes, histsize = NULL)
## S4 method for signature 'MultiWilcoxonTest':
summary(object, prior=1, significance=0.9, ...)
## S4 method for signature 'MultiWilcoxonTest':
hist(x, xlab='Rank Sum',
     ylab='Prob(Different | Y)', main='', ...)
## S4 method for signature 'MultiWilcoxonTest, missing':
plot(x, prior=1, significance=0.9,
     ylim=c(-0.5, 1), xlab='Rank Sum', ylab='Prob(Different | Y)', ...)
## S4 method for signature 'MultiWilcoxonTest':
cutoffSignificant(object, prior, significance, ...)
## S4 method for signature 'MultiWilcoxonTest':
selectSignificant(object, prior, significance, ...)
## S4 method for signature 'MultiWilcoxonTest':
countSignificant(object, prior, significance, ...)

```

## Arguments

|          |   |
|----------|---|
| data     | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes  | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| histsize | An integer; the number of bins used for the histogram summarizing the Wilcoxon statistics. When NULL, each discrete rank-sum value gets its own bin.  |
| object   | an object of the MultiWilcoxonTest class.   |
| x        | an object of the MultiWilcoxonTest class.   |

|                           |  |
|---------------------------|--|
| <code>xlab</code>         | Label for the x axis   |
| <code>ylab</code>         | Label for the y axis   |
| <code>ylim</code>         | Plotting limits on the y-axis  |
| <code>main</code>         | Graph title  |
| <code>prior</code>        | Prior probability that an arbitrary gene is not differentially expressed, or that an arbitrary row does not yield a significant Wilcoxon rank-sum statistic. |
| <code>significance</code> | Desired level of posterior probability   |
| <code>...</code>          | Additional graphical parameters.   |

### Details

See the paper by Efron and Tibshirani.

### Value

The standard methods `summary`, `hist`, and `plot` return what you would expect.

The `cutoffSignificant` method returns a list of two integers. Rank-sum values smaller than the first value or larger than the second value are statistically significant in the sense that their posterior probability exceeds the specified `significance` level given the assumptions about the prior probability of not being significant.

The `selectSignificant` method returns a vector of logical values identifying the significant test results, and `countSignificant` returns an integer counting the number of significant test results.

### Creating Objects

As usual, objects can be created by `new`, but better methods are available in the form of the `MultiWilcoxonTest` function. The inputs to this function are the same as those used for row-by-row statistical tests throughout the `ClassComparison` package; a detailed description can be found in the `MultiTtest` class.

The constructor computes row-by-row Wilcoxon rank-sum statistics on the input `data`, comparing the two groups defined by the `classes` argument. It also estimates the observed and theoretical (expected) density functions for the collection of rank-sum statistics.

The additional input argument, `histsize` is usually best left to its default value. In certain pathological cases, we have found it necessary to use fewer bins; one suspects that the underlying model does not adequately capture the complexity of those situations.

### Slots

**rank.sum.statistics:** A numeric vector containing the computed rank-sum statistics.

**xvals:** A numeric vector, best thought of as the vector of possible rank-sum statistics given the sizes of the two groups.

**theoretical.pdf:** A numeric vector containing the theoretical density function evaluated at the points of `xvals`.

**pdf:** A numeric vector containing the empirical density function computed at the points of `xvals`.

**unravel:** A numeric vector containing a smoothed estimate (by Poisson regression using B-splines) of the empirical density function evaluated at `xvals`.

**groups:** A vector containing the names of the groups defined by `classes`.

**call:** An object of class `call` representing the function call that created the object.

## Methods

**summary(object, prior=1, significance=0.9, ...)** Write out a summary of the object. For a given value of the `prior` probability of not being differentially expressed and a given significance cutoff on the posterior probability, reports the cutoffs and number of items in both tails of the distribution.

**hist(x, xlab='Rank Sum', ylab='Prob(Different|Y)', main='', ...)** Plot a histogram of the rank-sum statistics, with overlaid curves representing the expected and observed distributions. Colors of the curves are controlled by `COLOR.EXPECTED` and `COLOR.OBSERVED`.

**plot(x, prior=1, significance=0.9, ylim=c(-0.5, 1), xlab='Rank Sum', ylab='Prob(Different | Y)', ...)** Plots the posterior probability of being differentially expressed for given values of the `prior`. Horizontal lines are added at each specified `significance` level for the posterior probability.

**cutoffSignificant(object, prior, significance, ...)** Determine cutoffs on the rank-sum statistic at the desired significance level.

**selectSignificant(object, prior, significance, ...)** Compute a logical vector for selecting significant test results.

**countSignificant(object, prior, significance, ...)** Count the number of significant test results.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Efron B, Tibshirani R: Empirical bayes methods and false discovery rates for microarrays. *Genet Epidemiol* 2002, 23: 70-86.

Pounds S, Morris SW. Estimating the occurrence of false positives and false negatives in microarray studies by approximating and partitioning the empirical distribution of p-values. *Bioinformatics*. 2003 Jul 1;19(10):1236-42.

## See Also

Implementation is handled in part by the functions `dwil` and `rankSum`. The empirical Bayes results for alternative tests (such as `MultiTtest`) can be obtained using the beta-uniform mixture model in the `Bum` class.

## Examples

```
ng <- 10000
ns <- 15
nd <- 200
fake.class <- factor(rep(c('A', 'B'), each=ns))
fake.data <- matrix(rnorm(ng*ns*2), nrow=ng, ncol=2*ns)
fake.data[1:nd, 1:ns] <- fake.data[1:nd, 1:ns] + 2
fake.data[(nd+1):(2*nd), 1:ns] <- fake.data[(nd+1):(2*nd), 1:ns] - 2

a <- MultiWilcoxonTest(fake.data, fake.class)
hist(a)
plot(a)
plot(a, prior=0.85)
abline(h=0)
```

```
cutoffSignificant(a, prior=0.85, signif=0.95)
countSignificant(a, prior=0.85, signif=0.95)

# cleanup
rm(ng, ns, nd, fake.class, fake.data, a)
```

---

rankSum

*Wilcoxon Rank-Sum Statistic*

---

### Description

Compute the Wilcoxon rank-sum statistic

### Usage

```
rankSum(data, selector)
```

### Arguments

|          |   |
|----------|---|
| data     | A numeric vector                          |
| selector | A logical vector the same length as data. |

### Details

This is an efficient function to compute the value of the Wilcoxon rank-sum statistic without the extra overhead of the full `wilcox.test` function. It is used internally by the [MultiWilcoxonTest](#) class to perform rwo-by-row Wilcoxon tests.

### Value

Returns an integer, the rank-sum of the subset of the `data` for which the `selector` is true.

### Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

### See Also

[dwil](#), [MultiWilcoxonTest](#)

### Examples

```
dd <- rnorm(100)
cc <- rep(c(TRUE, FALSE), each=50)
rankSum(dd, cc)
rm(cc, dd)
```

Sam-class

*The Sam Class***Description**

Implements the "Significance Analysis of Microarrays" approach to detecting differentially expressed genes.

**Usage**

```
Sam(data, classes, nPerm = 100, verbose = TRUE)
## S4 method for signature 'Sam, missing':
plot(x, tracks=NULL, xlab='Expected T Statistics (Empirical)',
     ylab='Observed t Statistics', ...)
## S4 method for signature 'Sam':
summary(object, cutoff=1, ...)
## S4 method for signature 'Sam':
selectSignificant(object, cutoff=1, ...)
## S4 method for signature 'Sam':
countSignificant(object, cutoff=1, ...)
```

**Arguments**

|         |   |
|---------|---|
| data    | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| nPerm   | An integer; the number of permutations  |
| verbose | A logical flag  |
| x       | A Sam object  |
| tracks  | a numeric vector  |
| xlab    | Label for the x axis  |
| ylab    | Label for the y axis  |
| object  | A Sam object  |
| cutoff  | A numeric value   |
| ...     | The usual extra arguments to generic functions  |

**Details**

The SAM approach to analyzing microarray data was developed by Tusher and colleagues; their implementation is widely available. This is an independent implementation based on the description in their original paper, customized to use the same interface (and thus work with [ExpressionSet](#) objects) used by the rest of the [ClassComparison](#) package. The fundamental idea behind SAM is that the observed distribution of row-by-row two-sample t-tests should be compared not to the theoretical null distribution but to a null distribution estimated by a permutation test. The `Sam` constructor performs the permutation test.

**Value**

`summary` returns a `SamSummary` object.

`selectSignificant` returns a vector of logical values.

`countSignificant` returns an integer.

**Creating Objects**

As usual, objects can be created by `new`, but better methods are available in the form of the `Sam` function. The inputs to this function are the same as those used for row-by-row statistical tests throughout the `ClassComparison` package; a detailed description can be found in the `MultiTtest` class.

**Slots**

**t.statistics:** A numeric vector containing the observed t-statistics.

**observed:** A numeric vector containing the sorted observed t-statistics.

**expected:** A numeric vector of the expected distribution of t-statistics based on a permutation test.

**sim.data:** A matrix containing all the t-statistics from all the permutations.

**call:** The function `call` that created the object.

**Methods**

**summary(object, cutoff=1, ...)** Compute a summary of the object.

**plot(x, tracks=NULL, xlab='Expected T Statistics (Empirical)', ylab='Observed t Statistics', ...)**

Plot the observed and expected t-statistics. The `tracks` argument causes parallel lines to be drawn on either side of the quantile-quantile central line, at the specified offsets. Colors in the plot are controlled by the current values of `COLOR.CENTRAL.LINE` and `COLOR.CONFIDENCE.CURVE`

**selectSignificant(object, cutoff=1, ...)** Compute a vector that selects significant values

**countSignificant(object, cutoff=1, ...)** Count the number of significant values

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**References**

Tusher, V.G., Tibshirani, R., and Chu, G. 2001. Significance analysis of microarrays applied to the ionizing radiation response. *Proc Natl Acad Sci U S A* 98, 5116-5121.

**See Also**

`MultiTtest`, `Bum`

**Examples**

```

ng <- 10000
ns <- 50
nd <- 100
dat <- matrix(rnorm(ng*ns), ncol=ns)
dat[1:nd, 1:(ns/2)] <- dat[1:nd, 1:(ns/2)] + 2
dat[(nd+1):(2*nd), 1:(ns/2)] <- dat[(nd+1):(2*nd), 1:(ns/2)] - 2
cla <- factor(rep(c('A', 'B'), each=25))

res <- Sam(dat, cla)
plot(res)

plot(res, tracks=1:3)

summary(res)
summary(res, cutoff=2)

a <- summary(res)
plot(a@significant.calls)
plot(a@significant.calls[1:300])

countSignificant(res, 1)

rm(ng, ns, nd, dat, cla, res, a)

```

---

SamSummary-class     *The SamSummary Class*

---

**Description**

An implementation class. Users are not expected to create these objects directly; they are produced as return objects from the summary method for Sam.

**Slots**

**fdr:** A number between 0 and 1; the expected false discovery rate  
**hi:** Upper threshold for significance  
**lo:** Lower threshold for significance  
**cutoff:** A numeric value specified in the call to the Sam summary method.  
**significant.calls:** vector of logical values  
**average.false.count:** The average number of false positives in the permuted data at this cutoff level.

**Methods**

**show** signature(object = SamSummary): Print the object, which contains a summary of the underlying Sam object.

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**See Also**[Sam](#)**Examples**

```
# See the examples for the Sam class.
```

---

 significant

*Generic Functions for Significance*


---

**Description**

In the world of multiple testing that is inhabited by most microarray or protein profiling experiments, analysts frequently perform separate statistical tests for each gene or protein in the experiment. Determining cutoffs that achieve statistical significance (in a meaningful way) is an inherent part of the procedure. It is then common to select the significant items for further processing or for preparing reports, or at least to count the number of significant items. These generic functions provide a standard set of tools for selecting and counting the significant items, which can be used with various statistical tests and various ways to account for multiple testing.

**Usage**

```
cutoffSignificant(object, ...)
selectSignificant(object, ...)
countSignificant(object, ...)
```

**Arguments**

|                     |   |
|---------------------|---|
| <code>object</code> | Typically, an object that performs multiple statistical tests on microarray or proteomics data.                     |
| <code>...</code>    | All generic methods are designed to take optional additional arguments for flexibility in creating derived classes. |

**Value**

`cutoffSignificant` returns appropriate cutoff values that achieve specified significance criteria.

`selectSignificant` returns a logical vector, with true values indicating items that satisfy the cutoff making them statistically significant.

`countSignificant` returns an integer, representing the number of significant items.

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**See Also**

Classes that implement these methods include [Bum](#), [Sam](#), [Dudoit](#), [MultiWilcoxonTest](#), and [TNoM](#).

**Examples**

```
# Since these are generic methods, there are no examples. See the
# classes that implement specific instances.
```

---

SingleGroup-class *The SingleGroup Class*

---

**Description**

Preliminary analysis of one group of samples for use in the `SmoothTtest` class. A key feature is the standard quality control plot.

**Usage**

```
SingleGroup(avg, sd, span = 0.5, name = '')
## S4 method for signature 'SingleGroup':
as.data.frame(x, row.names=NULL, optional=FALSE)
## S4 method for signature 'SingleGroup':
summary(object, ...)
## S4 method for signature 'SingleGroup':
print(x, ...)
## S4 method for signature 'SingleGroup, missing':
plot(x, multiple=3, ccl=0, main=x@name,
      xlab='Mean', ylab='Std Dev', xlim=0, ylim=0, ...)
```

**Arguments**

|           |   |
|-----------|---|
| avg       | A numeric vector of mean values   |
| sd        | A numeric vector of standard deviations   |
| span      | The span parameter is passed onto <code>loess</code> .  |
| name      | A character string; the name of this object   |
| object    | A <code>SingleGroup</code> object   |
| x         | A <code>SingleGroup</code> object   |
| multiple  | A real number; the multiple of the smoothed standard deviation to call significant.   |
| ccl       | A list containing objects of the <code>ColorCoding</code> class. If left at its default value of zero, colors are chosen automatically. |
| main      | Plot title  |
| xlab      | Label for the x axis  |
| ylab      | Label for the y axis  |
| xlim      | Plotting limits for the x axis. If left at the default value of zero, then the limits are automatically generated                       |
| ylim      | Plotting limits for the y axis. If left at the default value of zero, then the limits are automatically generated                       |
| row.names | See the base version of <code>as.data.frame.default</code>  |
| optional  | See the base version of <code>as.data.frame.default</code>  |
| ...       | The usual extra parameters to generic or plotting routines  |

## Details

In 2001 and 2002, Baggerly and Coombes developed the smooth t-test for finding differentially expressed genes in microarray data. Along with many others, they began by log-transforming the data as a reasonable step in the direction of variance stabilization. They observed, however, that the gene-by-gene standard deviations still seemed to vary in a systematic way as a function of the mean log intensity. By borrowing strength across genes and using `loess` to fit the observed standard deviations as a function of the mean, one presumably got a better estimate of the true standard deviation.

## Creating Objects

Objects can be created by calls to the `SingleGroup` constructor. Users rarely have need to create these objects directly; they are usually created as a consequence of the construction of an object of the `SmoothTtest` class.

## Slots

**name:** A character string; the name of this object  
**avg:** The numeric vector of mean values  
**sd:** The numeric vector of standard deviations  
**span:** The `span` parameter used in the `loess` function to fit `sd` as a function of `avg`.  
**fit:** A list containing components `x` and `y` resulting from the `loess` fit.  
**score:** A numeric vector; the ratio of the pointwise standard deviations to their smooth (`loess`) estimates.

## Methods

**as.data.frame(x, row.names=NULL, optional=FALSE)** Combine the slots containing numeric vectors into a data frame, suitable for printing or exporting.

**summary(object, ...)** Write out a summary of the object.

**print(x, ...)** Print the entire object. You never want to do this.

**plot(x, multiple=3, ccl=0, main=x@name, xlab='Mean', ylab='Std Dev', xlim=0, ylim=0, ...)** Produce a scatter plot of the standard deviations (`x@sd`) as a function of the means (`x@avg`). The appropriate multiple of the `loess` fit is overlaid, and points that exceed this multiple are flagged in a different color. Colors in the plot are controlled by the current values of `COLOR.CENTRAL.LINE`, `COLOR.CONFIDENCE.CURVE`, `COLOR.BORING`, `COLOR.BAD.REPLICATE`, and `COLOR.WORST.REPLIC`.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Baggerly, K.A., Coombes, K.R., Hess, K.R., Stivers, D.N., Abruzzo, L.V., Zhang, W. Identifying differentially expressed genes in cDNA microarray experiments. *J Comp Biol.* 8:639-659, 2001.

Coombes, K.R., Highsmith, W.E., Krogmann, T.A., Baggerly, K.A., Stivers, D.N., Abruzzo, L.V. Identifying and quantifying sources of variation in microarray data using high-density cDNA membrane arrays. *J Comp Biol.* 9:655-669, 2002.

**See Also**[SmoothTtest](#)**Examples**

```

m <- rnorm(1000, 8, 2.5)
v <- rnorm(1000, 0.7)
plot(m, v)

x <- SingleGroup(m, v, name='bogus')

summary(x)

plot(x)
plot(x, multiple=2)

# cleanup
rm(m, v, x)

```

---

SmoothTtest-class *The SmoothTtest Class*

---

**Description**

Implements the smooth t-test for differential expression as developed by Baggerly and Coombes.

**Usage**

```

SmoothTtest(stats, aname = 'Group One', bname = 'Group Two',
  name = paste(aname, 'vs.', bname))
## S4 method for signature 'SmoothTtest':
as.data.frame(x, row.names=NULL, optional=FALSE)
## S4 method for signature 'SmoothTtest':
summary(object, ...)
## S4 method for signature 'SmoothTtest, missing':
plot(x, folddiff=3, goodflag=2, badch=4, ccl=0,
  name=x@name, pch='.', xlab='log intensity', ylab='log ratio', ...)

```

**Arguments**

|           |   |
|-----------|---|
| stats     | An object of the <a href="#">TwoGroupStats</a> class.   |
| aname     | A character string; the name of the second group  |
| bname     | A character string; the name of the second group  |
| name      | A character string; the name of this object   |
| object    | A <a href="#">SmoothTtest</a> object  |
| x         | A <a href="#">SmoothTtest</a> object  |
| row.names | See the base version of <a href="#">as.data.frame.default</a>                                     |
| optional  | See the base version of <a href="#">as.data.frame.default</a>                                     |
| folddiff  | A real number; the level of fold difference considered large enough to be indicated in the plots. |

|                       |   |
|-----------------------|---|
| <code>goodflag</code> | A real number; the level (in standard deviation units) of the smooth t-statistic considered large enough to be indicated in the plot.   |
| <code>badch</code>    | A real number; the level of variability in single groups considered large enough to be worrisome. See the <code>multiple</code> argument to the <code>plot</code> method in the <code>SingleGroup</code> class. |
| <code>ccl</code>      | A list containing objects of the <code>ColorCoding</code> class. If left at its default value of zero, colors are chosen automatically.   |
| <code>pch</code>      | Default plotting character  |
| <code>xlab</code>     | Label for the x axis  |
| <code>ylab</code>     | Label for the y axis  |
| <code>...</code>      | The usual extra parameters to generic or plotting routines  |

### Details

In 2001 and 2002, Baggerly and Coombes developed the smooth t-test for finding differentially expressed genes in microarray data. Along with many others, they began by log-transforming the data as a reasonable step in the direction of variance stabilization. They observed, however, that the gene-by-gene standard deviations still seemed to vary in a systematic way as a function of the mean log intensity. By borrowing strength across genes and using `loess` to fit the observed standard deviations as a function of the mean, one presumably got a better estimate of the true standard deviation.

These smooth estimates are computed for each of two groups of samples being compared. They are then combined (gene-by-gene using the usual univariate formulas) to compute pooled "smooth" estimates of the standard deviation. These smooth estimates are then used in gene-by-gene t-tests.

The interesting question then arises of how to compute and interpret p-values associated to these individual tests. The liberal argument asserts that, because smoothing uses data from hundreds of measurements to estimate the standard deviation, it can effectively be treated as "known" in the t-tests, which should thus be compared against the normal distribution. A conservative argument claims that the null distribution should still be the t-distribution with the degrees of freedom determined in the usual way by the number of samples. The truth probably lies somewhere in between, and is probably best approximated by some kind of permutation test. In this implementation, we take the coward's way out and don't provide any of those alternatives. You have to extract the t-statistics (from the `smooth.t.statistics` slot of the object) and compute your own p-values in your favorite way. If you base the computations on a theoretical model rather than a permutation test, then the `Bum` class provides a convenient way to account for multiple testing.

### Creating Objects

In practice, users will first use a data frame and a classification vector (or an `ExpressionSet`) to construct an object of the `TwoGroupStats` object. This object can then be handed directly to the `SmoothTtest` function to perform the smooth t-test.

### Slots

**one:** An object of the `SingleGroup` class representing a loess smooth of standard deviation as a function of the mean in the first group of samples.

**two:** An object of the `SingleGroup` class representing a loess smooth of standard deviation as a function of the mean in the second group of samples.

**smooth.t.statistics:** A numeric vector containing the smooth t-statistics

**fit:** A data.frame containing two columns, x and y, containing the smooth estimates of the pooled standard deviation

**dif:** A numeric vector of the differences in mean values between the two groups

**avg:** A numeric vector of the overall mean value

**aname:** A character string; the name of the first group

**bname:** A character string; the name of the second group

**name:** A character string; the name of this object

**stats:** The `TwoGroupStats` object that was used to create this object.

## Methods

**as.data.frame(x, row.names=NULL, optional=FALSE)** Convert the object into a data frame suitable for printing or exporting.

**summary(object, ...)** Write out a summary of the object.

**plot(x, folddiff=3, goodflag=2, badch=4, ccl=0, name=x@name, pch='.', xlab='log intensity', ylab='log ratio', ...)**  
 Create a set of six plots. The first two plots are the QC plots from the `SingleGroup` objects representing the two groups of samples. The third plot is a scatter plot comparing the means in the two groups. The fourth plot is Bland-Altman plot of the overall mean against the difference in means (also known colloquially as an M-vs-A plot). The fifth plot is a histogram of the smooth t-statistics. The final plot is a scatter plot of the smooth t-statistics as a function of the mean intensity. Colors in the plots are controlled by the current values of `COLOR.BORING`, `COLOR.SIGNIFICANT`, `COLOR.BAD.REPLICATE`, `COLOR.WORST.REPLICATE`, `COLOR.FOLD.DIFFERENCE`, `COLOR.CENTRAL.LINE`, AND `COLOR.CONFIDENCE.CURVE`.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Baggerly, K.A., Coombes, K.R., Hess, K.R., Stivers, D.N., Abruzzo, L.V., Zhang, W. Identifying differentially expressed genes in cDNA microarray experiments. *J Comp Biol.* 8:639-659, 2001.

Coombes, K.R., Highsmith, W.E., Krogmann, T.A., Baggerly, K.A., Stivers, D.N., Abruzzo, L.V. Identifying and quantifying sources of variation in microarray data using high-density cDNA membrane arrays. *J Comp Biol.* 9:655-669, 2002.

Altman DG, Bland JM. Measurement in Medicine: the Analysis of Method Comparison Studies. *The Statistician*, 1983; 32: 307-317.

## See Also

[Bum](#), [MultiTtest](#), [SingleGroup](#), [TwoGroupStats](#).

## Examples

```
bogus <- matrix(rnorm(30*1000, 8, 3), ncol=30, nrow=1000)
splitter <- rep(FALSE, 30)
splitter[16:30] <- TRUE
x <- TwoGroupStats(bogus, splitter)
y <- SmoothTtest(x)

opar <- par(mfrow=c(2, 3), pch='.')
```

```

plot(y, badch=2, goodflag=1)
par(opar)

# cleanup
rm(bogus, splitter, x, y, opar)

```

---

TNoM-class

*The TNoM and fullTNoM Classes*


---

### Description

Implements the "Total Number of Misclassifications" method for finding differentially expressed genes.

### Usage

```

TNoM(data, classes, verbose = TRUE)
## S4 method for signature 'TNoM':
summary(object, ...)
## S4 method for signature 'TNoM':
update(object, nPerm, verbose=FALSE, ...)
## S4 method for signature 'TNoM':
selectSignificant(object, cutoff, ...)
## S4 method for signature 'TNoM':
countSignificant(object, cutoff, ...)

## S4 method for signature 'fullTNoM, missing':
plot(x, ...)
## S4 method for signature 'fullTNoM':
hist(x, ...)

```

### Arguments

|         |   |
|---------|---|
| data    | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| verbose | A logical flag; whether to print out intermediate results   |
| object  | A TNoM object   |
| nPerm   | An integer; the number of permutations to perform   |
| cutoff  | An integer  |
| x       | A fullTNoM object   |
| ...     | Additional plotting or other arguments.   |

## Details

The TNoM method was developed by Yakhini and Ben-Dor and first applied in the melanoma microarray study by Bittner and colleagues (see references). The goal of the method is to detect genes that are differentially expressed between two groups of samples. The idea is that each gene serves as a potential classifier to distinguish the two groups. One starts by determining an optimal cutoff on the expression of each gene and counting the number of misclassifications that gene makes. Next, we bin genes based on the total number of misclassifications. This distribution can be compared with the expected value (by simulating normal data sets of the same size). Alternatively, one can estimate the null distribution directly by scrambling the sample labels to perform a permutation test.

The TNoM constructor computes the optimal cutoffs and the misclassification rates. The `update` method performs the simulations and permutation tests, producing an object of the `fullTNoM` class.

## Value

`summary` returns a `TNoMSummary` object.

`update` returns a `fullTNoM` object.

`selectSignificant` returns a vector of logical values.

`countSignificant` returns an integer.

## Creating Objects

As usual, objects can be created by `new`, but better methods are available in the form of the `TNoM` function. The inputs to this function are the same as those used for row-by-row statistical tests throughout the `ClassComparison` package; a detailed description can be found in the `MultiTtest` class.

## Slots

Objects of the `TNoM` class have the following slots:

**data:** The data matrix used to construct the object

**tnomData:** A numeric vector, whose length is the number of rows in `data`, recording the minimum number of misclassification achieved using this data row.

**nCol:** The number of columns in `data`

**nRow:** The number of rows in `data`

**classifier:** The classification vector used to create the object.

**call:** The function `call` that created the object

Objects of the `fullTNoM` class have the following slots:

**dex:** Numeric vector of the different possible numbers of misclassifications

**fakir:** Numeric vector of expected values based on simulations

**obs:** Numeric vector of observed values

**scr:** Numeric vector of values based on a permutation test

**name:** A character string with a name for the object

## Methods

Objects of the `TNoM` class have the following methods:

**summary(object, ...)** Write out a summary of the object, including the number of genes achieving each possible number of misclassifications.

**countSignificant(object, cutoff, ...)** Count the number of significant genes at the given `cutoff`.

**selectSignificant(object, cutoff, ...)** Get a vector for selecting the number of significant genes at the given `cutoff`.

**update(object, nPerm, verbose=FALSE, ...)** Perform simulation and permutation tests on the `TNoM` object.

Objects of the `fullTNoM` class have the following methods:

**plot(x, ...)** Plot a summary of the `TNoM` object. This consists of three curves: the observed cumulative number of genes at each misclassification level, along with the corresponding numbers expected based on simulations or permutation tests. The colors of the curves are controlled by the values of `COLOR.OBSERVED`, `COLOR.EXPECTED`, and `COLOR.PERMTEST`

**hist(x, ...)** Plot a not terribly useful nor informative histogram of the results.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Bittner M, Meltzer P, Chen Y, Jiang Y, Seftor E, Hendrix M, Radmacher M, Simon R, Yakhini Z, Ben-Dor A, Sampas N, Dougherty E, Wang E, Marincola F, Gooden C, Lueders J, Glatfelter A, Pollock P, Carpten J, Gillanders E, Leja D, Dietrich K, Beaudry C, Berens M, Alberts D, Sondak V. Molecular classification of cutaneous malignant melanoma by gene expression profiling. *Nature*. 2000 Aug 3;406(6795):536-40.

## See Also

[MultiTtest](#), [MultiWilcoxonTest](#), [Bum](#)

## Examples

```
n.genes <- 200
n.samples <- 10

bogus <- matrix(rnorm(n.samples*n.genes, 0, 3), ncol=n.samples)
splitter <- rep(FALSE, n.samples)
splitter[sample(1:n.samples, trunc(n.samples/2))] <- TRUE

tn <- TNoM(bogus, splitter)
summary(tn)

tnf <- update(tn)
plot(tnf)
hist(tnf)

rm(bogus, splitter, n.genes, n.samples, tn, tnf)
```

---

TNoMSummary-class *The TNoMSummary Class*

---

### Description

An implementation class. Users are not expected to create these objects directly; they are produced as return objects from the summary method for TNoM.

### Slots

**TNoM:** Object of class TNoM ~~

**counts:** Object of class numeric ~~

### Methods

**show** signature(object = TNoMSummary): Print the object, which contains a summary of the underlying TNoM object. In particular, the summary reports the number of genes achieving each possible number of misclassifications.

### Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

### See Also

[TNoM](#)

### Examples

```
# See the examples for the TNoM class.
```

---

TwoGroupStats-class  
*The TwoGroupStats Class*

---

### Description

Compute row-by-row means and variances for a data matrix whose columns belong to two different groups of interest.

### Usage

```
TwoGroupStats(data, classes, name = comparison, name1 = A, name2 = B)
## S4 method for signature 'TwoGroupStats':
as.data.frame(x, row.names=NULL, optional=FALSE)
## S4 method for signature 'TwoGroupStats':
summary(object, ...)
## S4 method for signature 'TwoGroupStats':
print(x, ...)
## S4 method for signature 'TwoGroupStats, missing':
plot(x, main=x@name, useLog=FALSE, ...)
```

**Arguments**

|                        |   |
|------------------------|---|
| <code>data</code>      | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| <code>classes</code>   | If <code>data</code> is a data frame or matrix, then <code>classes</code> must be either a logical vector or a factor. If <code>data</code> is an <a href="#">ExpressionSet</a> , then <code>classes</code> can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| <code>name</code>      | A character string; the name of this object   |
| <code>name1</code>     | A character string; the name of the first group   |
| <code>name2</code>     | A character string; the name of the second group  |
| <code>x</code>         | A <code>TwoGroupStats</code> object   |
| <code>row.names</code> | See the base version of <a href="#">as.data.frame.default</a>   |
| <code>optional</code>  | See the base version of <a href="#">as.data.frame.default</a>   |
| <code>object</code>    | A <code>TwoGroupStats</code> object   |
| <code>main</code>      | Plot title  |
| <code>useLog</code>    | a logical flag; should the values be log-transformed before plotting?   |
| <code>...</code>       | The usual extra arguments to generic functions  |

**Details**

This class was one of the earliest developments in our suite of tools to analyze microarrays. Its main purpose is to segregate out the preliminary computation of summary statistics on a row-by-row basis, along with a set of plots that could be generated automatically and used for quality control.

**Creating Objects**

As usual, objects can be created by `new`, but better methods are available in the form of the `TwoGroupStats` function. The inputs to this function are the same as those used for row-by-row statistical tests throughout the `ClassComparison` package; a detailed description can be found in the `MultiTtest` class.

One should note that this class serves as the front end to the [SmoothTtest](#) class, providing it with an interface that accepts [ExpressionSet](#) objects compatible with the other statistical tests in the `ClassComparison` package.

**Slots**

- mean1:** The numeric vector of means in the first group
- mean2:** The numeric vector of means in the second group
- overallMean:** The numeric vector of overall row means
- var1:** The numeric vector of variances in the first group
- var2:** The numeric vector of variances in the second group
- overallVar:** The numeric vector of variances assuming the two groups have the same mean
- pooledVar:** The numeric vector of row-by-row pooled variances, assuming the two groups have the same variance but different means
- n1:** The number of items in the first group

**n2:** The number of items in the first group  
**name1:** The name of the first group  
**name2:** The name of the second group  
**name:** The name of the object

## Methods

**as.data.frame(x, row.names=NULL, optional=FALSE)** Collect the numeric vectors from the object into a single data frame, suitable for printing or exporting.

**summary(object, ...)** Write out a summary of the object.

**print(x, ...)** Print the object. (Actually, it only prints a summary, since the whole object is almost always more than you really want to see. If you insist on printing everything, use `as.data.frame()`.)

**plot(x, main=x@name, useLog=FALSE, ...)** This function actually produces six different plots of the data, so it is usually wrapped by a graphical layout command like `par(mfrow=c(2,3))`. The first two plots show the relation between the mean and standard deviation for the two groups separately; the third plot does the same for the overall mean and variance. The fourth plot is a Bland-Altman plot of the difference between the means against the overall mean. (In the microarray world, this is usually called an M-vs-A plot.) A loess fit is overlaid on the scatter plot, and points outside confidence bounds based on the fit are printed in a different color to flag them as highly variable. The fifth plot shows a loess fit (with confidence bounds) of the difference as a function of the row index (which often is related to the geometric position of spots on a microarray). Thus, this plot gives a possible indication of regions of an array where unusual things happen. The final plot compares the overall variances to the pooled variances.

## Author(s)

Kevin R. Coombes <kcoombes@mdanderson.org>

## References

Altman DG, Bland JM. Measurement in Medicine: the Analysis of Method Comparison Studies. *The Statistician*, 1983; 32: 307-317.

## See Also

[SmoothTtest](#), [MultiTtest](#)

## Examples

```
bogus <- matrix(rnorm(30*1000, 8, 3), ncol=30, nrow=1000)
splitter <- rep(FALSE, 30)
splitter[16:30] <- TRUE

x <- TwoGroupStats(bogus, splitter)
summary(x)

opar<-par(mfrow=c(2,3), pch='.')
plot(x)
par(opar)

# cleanup
rm(bogus, splitter, x, opar)
```

variantT

*Classes for Variant T-tests***Description**

Class to perform row-by-row paired or unequal variance t-tests on microarray or proteomics data.

**Usage**

```
MultiTtestPaired(data, classes, pairing)
MultiTtestUnequal(data, classes)
## S4 method for signature 'MultiTtestPaired':
summary(object, ...)
## S4 method for signature 'MultiTtestUnequal':
summary(object, ...)
```

**Arguments**

|         |   |
|---------|---|
| data    | Either a data frame or matrix with numeric values or an <a href="#">ExpressionSet</a> as defined in the BioConductor tools for analyzing microarray data.   |
| classes | If data is a data frame or matrix, then classes must be either a logical vector or a factor. If data is an <a href="#">ExpressionSet</a> , then classes can be a character string that names one of the factor columns in the associated <a href="#">phenoData</a> subobject. |
| pairing | A numerical vector indicating which samples are paired.   |
| object  | A <a href="#">MultiTtest</a> object   |
| ...     | Unused; optional extra parameters for <code>summary</code> .  |

**Creating objects**

Although objects can be created using `new`, the better method is to use the `MultiTtestPaired` or `MultiTtestUnequal` functions. In the simplest case, you simply pass in a data matrix and a logical vector assigning classes to the columns (and, in the case of a paired t-test, a numeric vector describing the pairing), and the constructor performs row-by-row two-sample t-tests and computes the associated (single test) p-values. To adjust for multiple testing, you can pass the p-values on to the [Bum](#) class.

If you use a factor instead of a logical vector, then the t-test compares the first level of the factor to everything else. To handle the case of multiple classes, see the [MultiLinearModel](#) class.

As with other class comparison functions that are part of the OOMPA, we can also perform statistical tests on [ExpressionSet](#) objects from the BioConductor libraries. In this case, we pass in an [ExpressionSet](#) object along with the name of a factor to use for splitting the data.

**Extends**

Both classes extend class [MultiTtest](#), directly. See that class for descriptions of the inherited methods and slots.

**Slots**

**df:** The `MultiTtestUnequal` class adds a slot to record the gene-by-gene degrees of freedom, which can change along with the variances.

**Methods**

**summary** signature(object = MultiTtestPaired): Write out a summary of the object.

**summary** signature(object = MultiTtestUnequal): Write out a summary of the object.

**Author(s)**

Kevin R. Coombes <kcoombes@mdanderson.org>

**References**

None.

**See Also**

[MultiTtest](#), [Bum](#)

**Examples**

```
ng <- 10000
ns <- 50
dat <- matrix(rnorm(ng*ns), ncol=ns)
cla <- factor(rep(c('A', 'B'), each=25))
res <- MultiTtestUnequal(dat, cla)
summary(res)
hist(res, breaks=101)
plot(res, res@p.values)

pairing <- rep(1:25, 2)
res <- MultiTtestPaired(dat, cla, pairing)
summary(res)
plot(res)
hist(res@p.values, breaks=101)

rm(ng, ns, dat, cla, res, pairing)
```

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